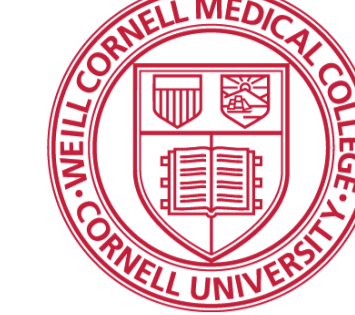


Natural scene statistics relate to perceptual salience of second-, third-, and fourth-order spatial correlations



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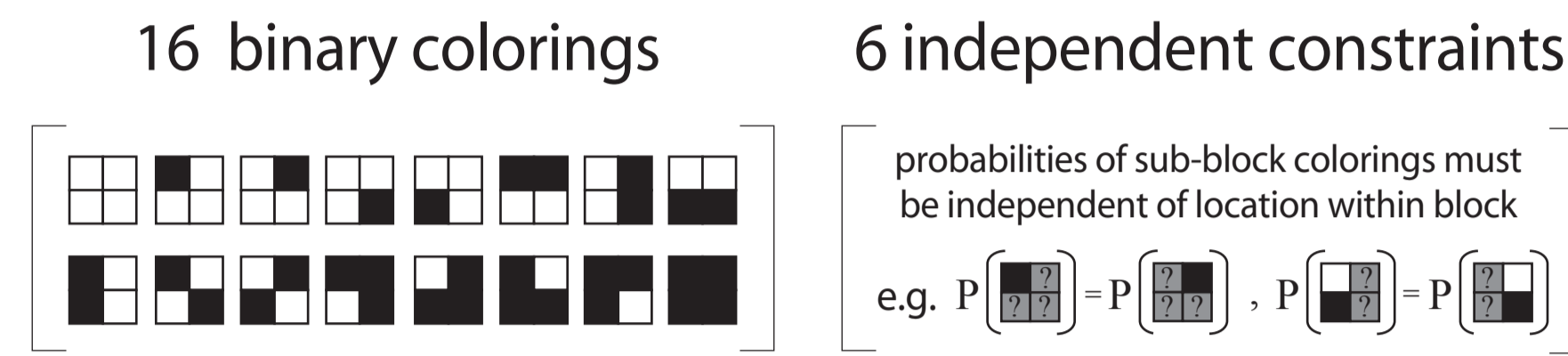
ABSTRACT

The statistical regularities of natural signals provide insight into characteristics of early visual processing (e.g. the center-surround receptive fields of retinal ganglion cells). Can the match between natural signal statistics and neural processing mechanisms be extended beyond the sensory periphery?

Recent work, which revealed that human sensitivity to isodipole synthetic textures is closely related to the structure of fourth-order spatial correlations in natural scenes [1], leads us to propose the following organizing principle:

The perceptual salience of visual textures increases with the variance, or unpredictability, of the corresponding correlations over the ensemble of natural scenes.

BINARY TEXTURE SPACE



10 independent coordinates:

(1) First-order luminance coordinate (γ)
 $\gamma = +P(\blacksquare) - P(\square)$

(4) Second-order coordinates for pairwise correlations ($\beta_1, \beta_-, \beta_v, \beta_r$)

$\beta_1 = +P(\begin{smallmatrix} \blacksquare & \blacksquare \\ \blacksquare & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \square \\ \blacksquare & \square \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare \\ \square & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square \\ \square & \square \end{smallmatrix})$

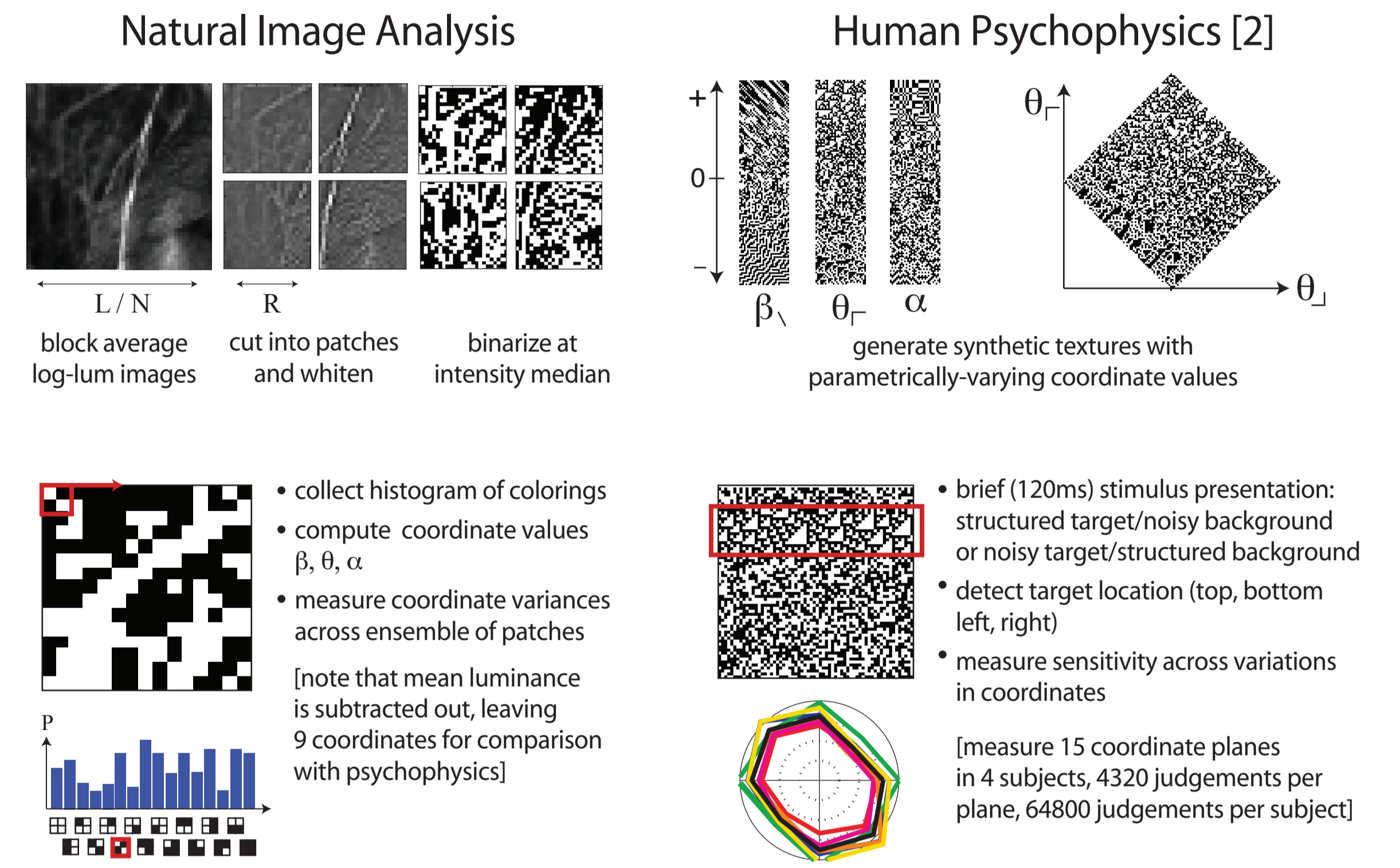
(4) Third-order luminance coordinates for parity of triplets ($\theta_r, \theta_-, \theta_v, \theta_+$)

$\theta_r = +P(\begin{smallmatrix} \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \blacksquare & \square \\ \blacksquare & \blacksquare & \square \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \square & \blacksquare \\ \blacksquare & \square & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \blacksquare & \square & \square \\ \blacksquare & \square & \square \end{smallmatrix}) + P(\begin{smallmatrix} \square & \blacksquare & \blacksquare \\ \square & \blacksquare & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare & \square \\ \square & \blacksquare & \square \end{smallmatrix}) - P(\begin{smallmatrix} \square & \square & \blacksquare \\ \square & \square & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square & \square \\ \square & \square & \square \end{smallmatrix})$

(1) Fourth-order coordinate for parity of quadruplets (α)

$\alpha = +P(\begin{smallmatrix} \blacksquare & \blacksquare & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \blacksquare & \blacksquare & \square \\ \blacksquare & \blacksquare & \blacksquare & \square \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \blacksquare & \square & \blacksquare \\ \blacksquare & \blacksquare & \square & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \blacksquare & \blacksquare & \square & \square \\ \blacksquare & \blacksquare & \square & \square \end{smallmatrix}) + P(\begin{smallmatrix} \blacksquare & \square & \blacksquare & \blacksquare \\ \blacksquare & \square & \blacksquare & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \blacksquare & \square & \blacksquare & \square \\ \blacksquare & \square & \blacksquare & \square \end{smallmatrix}) + P(\begin{smallmatrix} \blacksquare & \square & \square & \blacksquare \\ \blacksquare & \square & \square & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \blacksquare & \square & \square & \square \\ \blacksquare & \square & \square & \square \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare & \blacksquare & \blacksquare \\ \square & \blacksquare & \blacksquare & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare & \blacksquare & \square \\ \square & \blacksquare & \blacksquare & \square \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare & \square & \blacksquare \\ \square & \blacksquare & \square & \blacksquare \end{smallmatrix}) - P(\begin{smallmatrix} \square & \blacksquare & \square & \square \\ \square & \blacksquare & \square & \square \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square & \blacksquare & \blacksquare \\ \square & \square & \blacksquare & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square & \blacksquare & \square \\ \square & \square & \blacksquare & \square \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square & \square & \blacksquare \\ \square & \square & \square & \blacksquare \end{smallmatrix}) + P(\begin{smallmatrix} \square & \square & \square & \square \\ \square & \square & \square & \square \end{smallmatrix})$

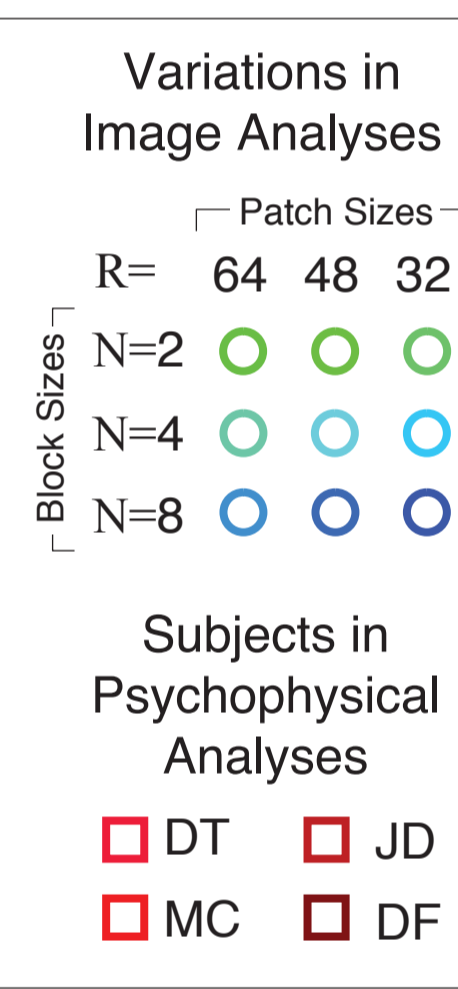
ANALYSIS METHODS



GENERAL APPROACH

We compare the following between natural image and psychophysical data:

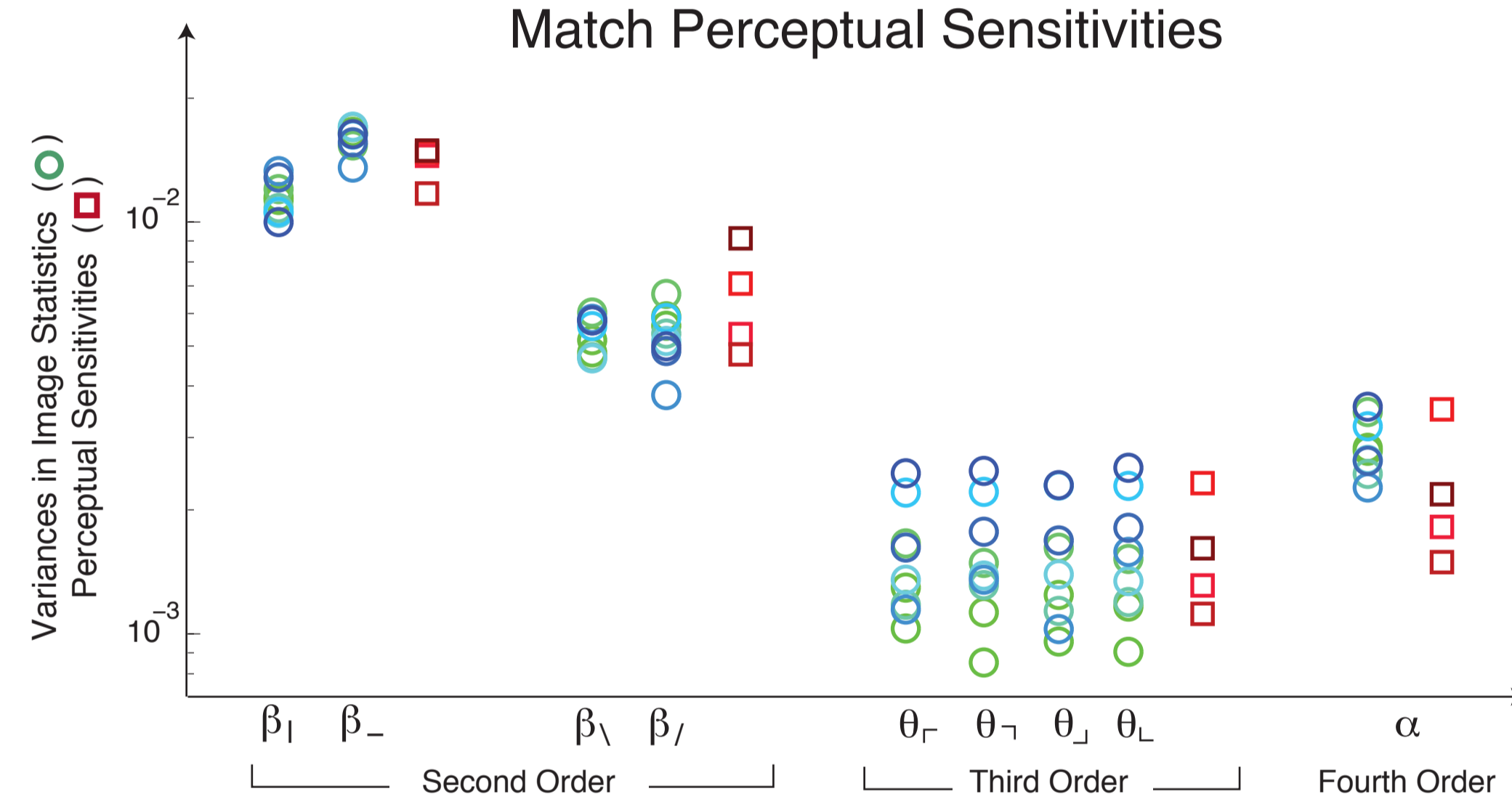
- Single statistics (upper right): Variances in image statistics versus perceptual sensitivities
- Pairwise statistic planes (lower left): inverse covariances in image statistics versus perceptual thresholds
- Full 9D space of statistics (lower right): principal components of image statistic variances versus principal components inferred from psychophysical isodiscrimination contours



Note that there is an overall scale difference between image and psychophysical analyses. Each image analysis was rescaled by a single factor chosen to minimize the least squared error (summed over all 9 statistics) between image variances and perceptual sensitivities.

SINGLE STATISTICS

Order and Magnitude of Natural Image Variances Match Perceptual Sensitivities



CONCLUSIONS

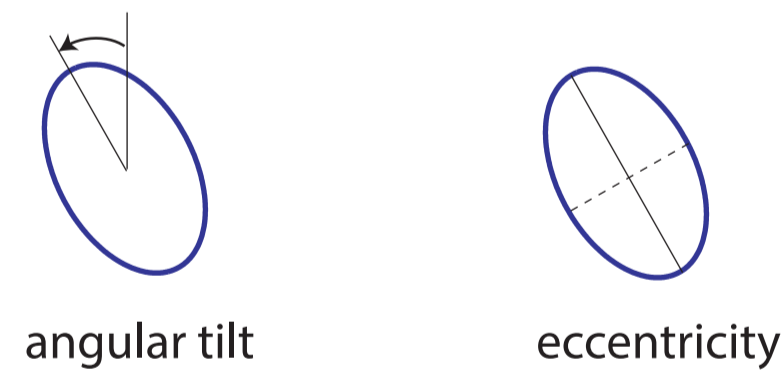
Variances in natural image statistics match perceptual sensitivities:

- Order and magnitude of variances match order and magnitude of perceptual sensitivities
- Features of 9D space of covariances (including pairwise plane projections and principal components) match the features of 9D space of sensitivities

These results suggest that central neural mechanisms are efficiently tuned to higher-order statistics of natural scenes.

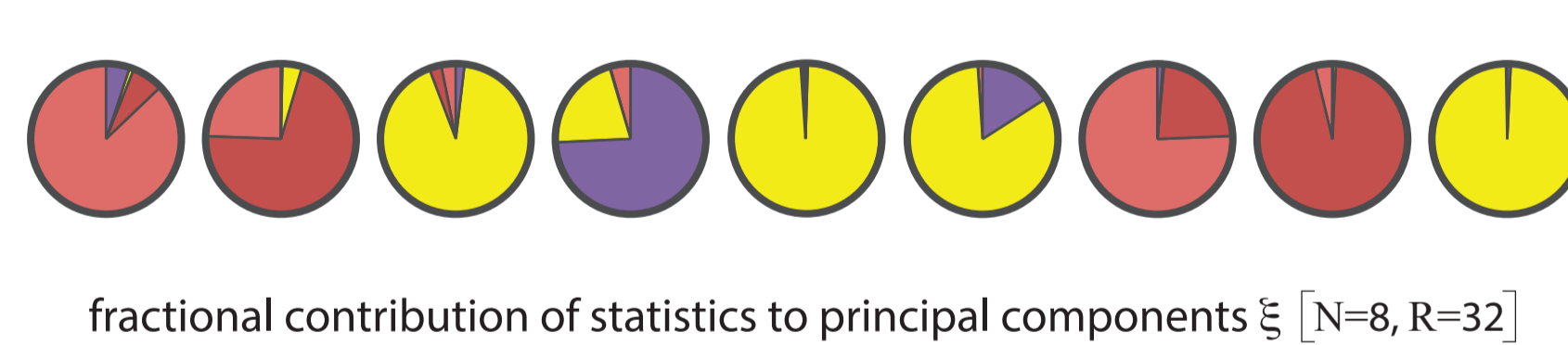
PAIRS OF STATISTICS

compare properties of inverse covariance ellipses and psychophysical thresholds in pairwise statistic planes



FULL 9D SPACE OF STATISTICS

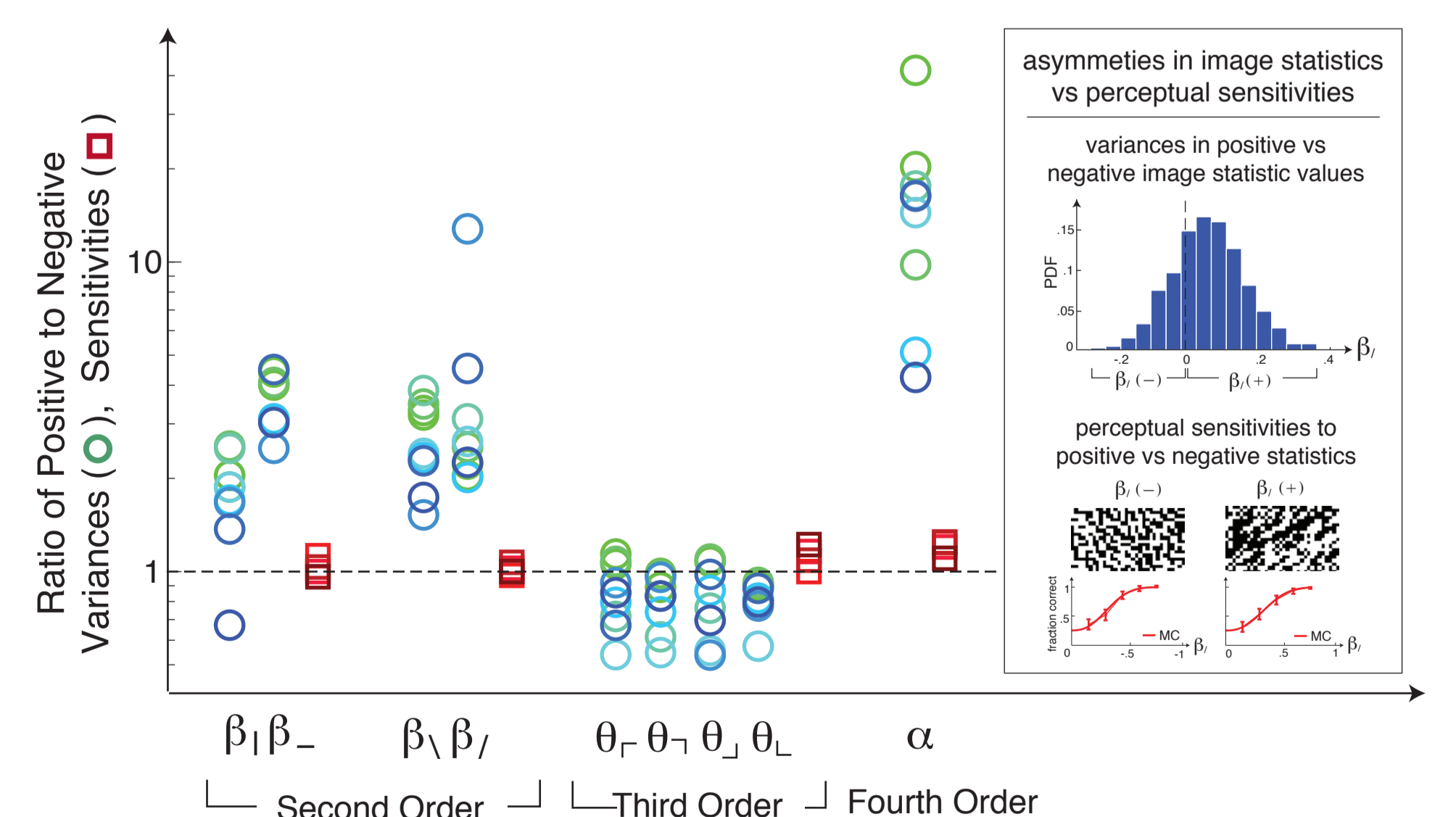
compare relative contributions of different statistics to principal components of natural image and psychophysical analyses



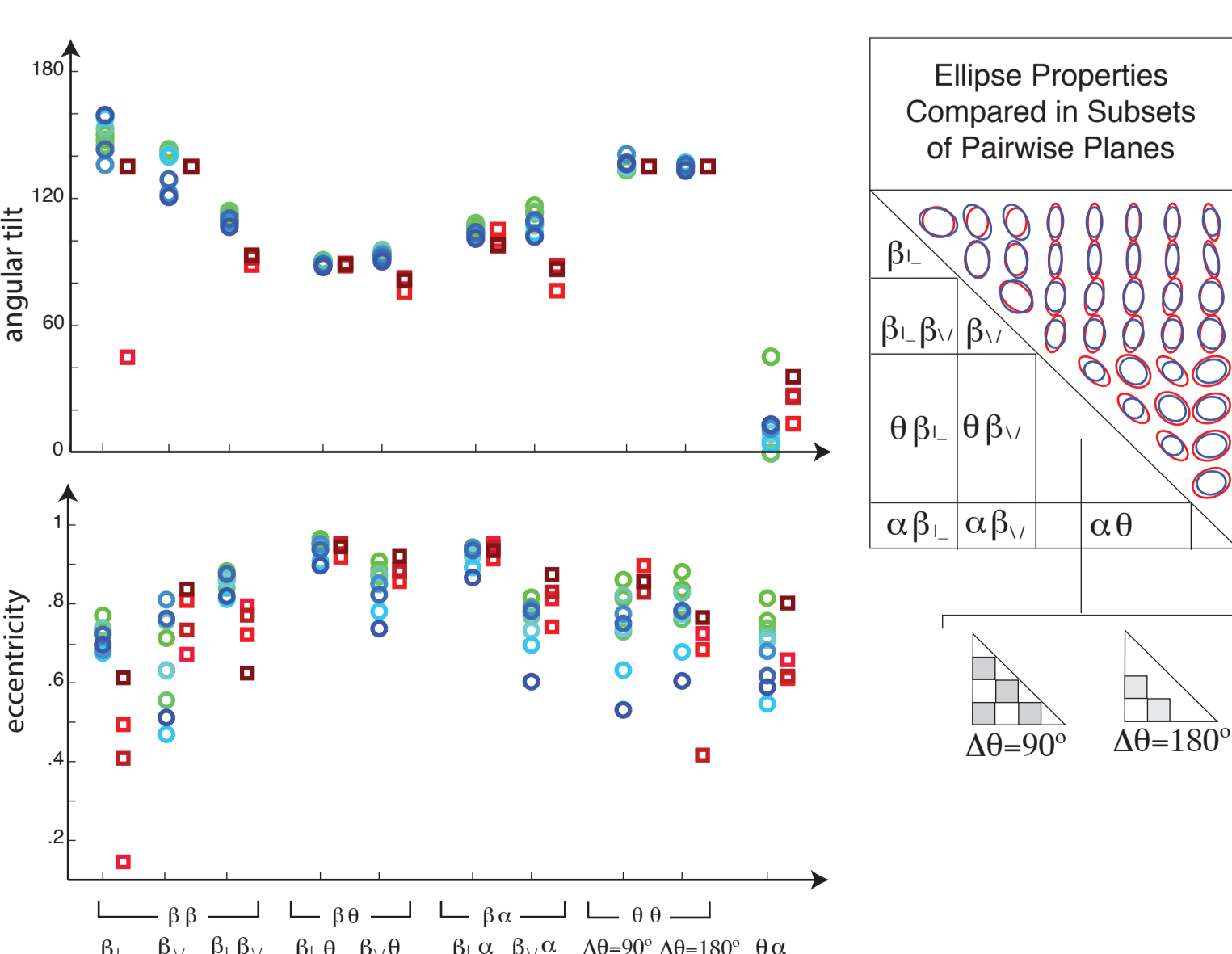
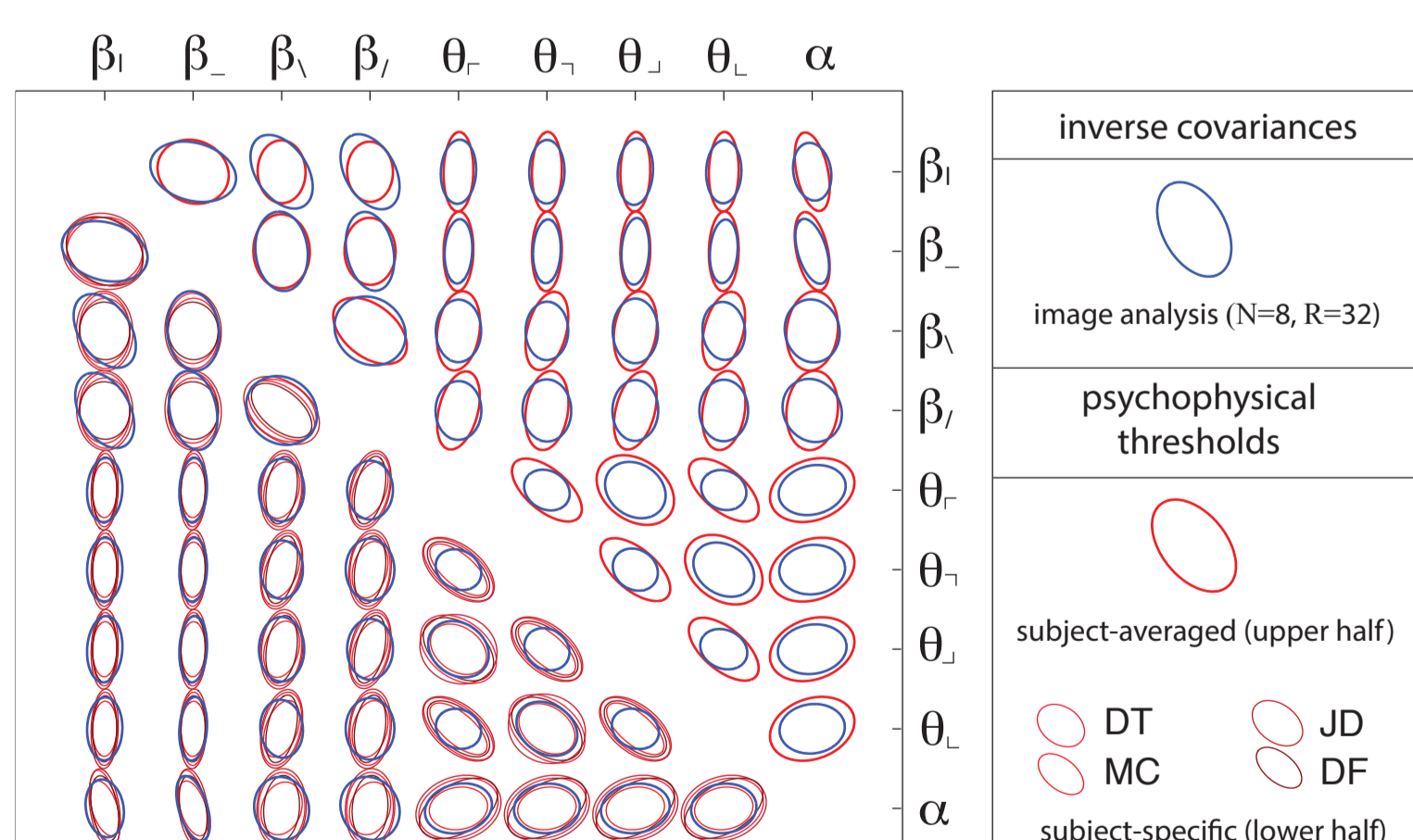
FURTHER QUESTIONS

Systematic differences (mostly small) between natural image statistics and perceptual sensitivities:

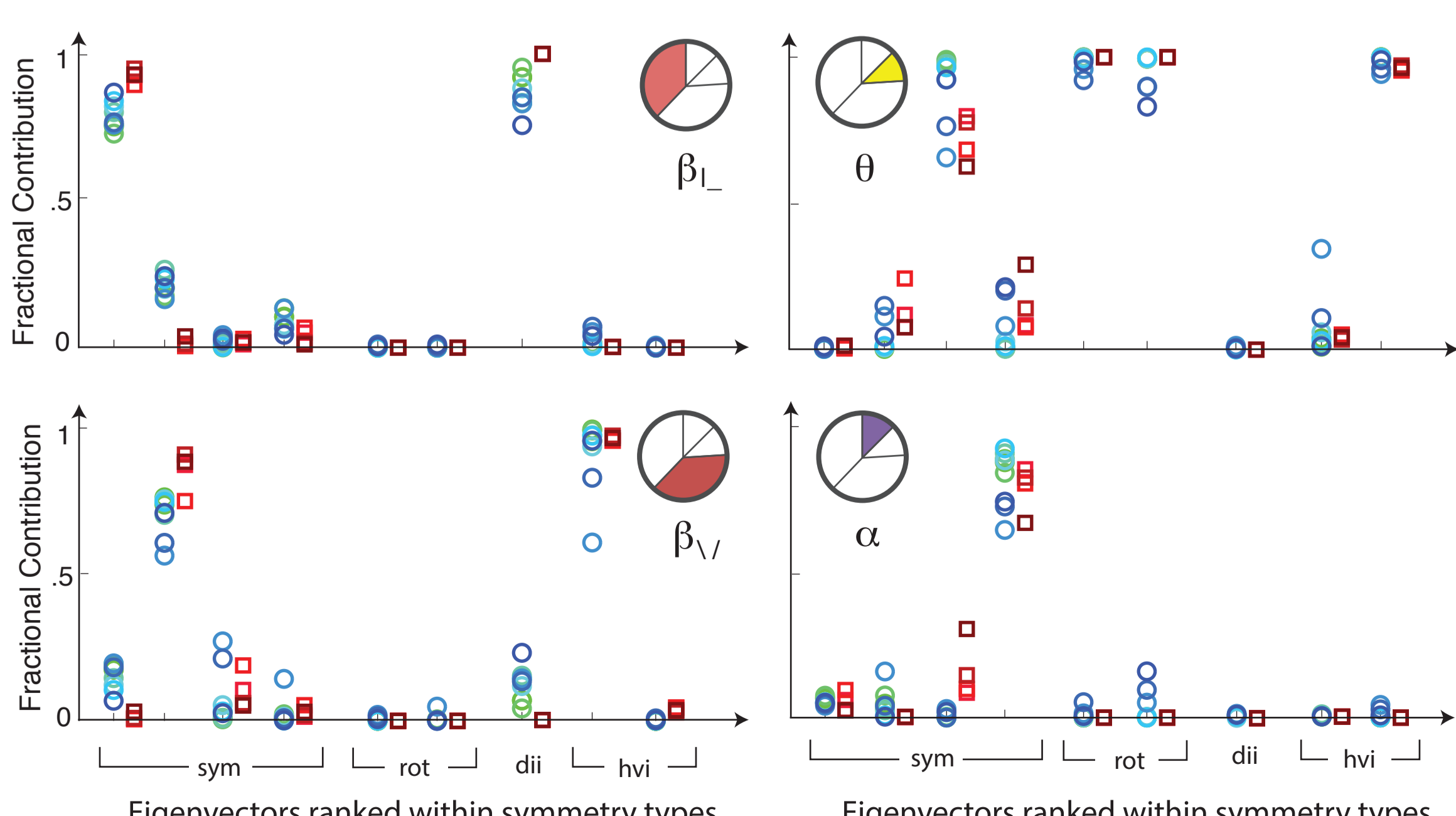
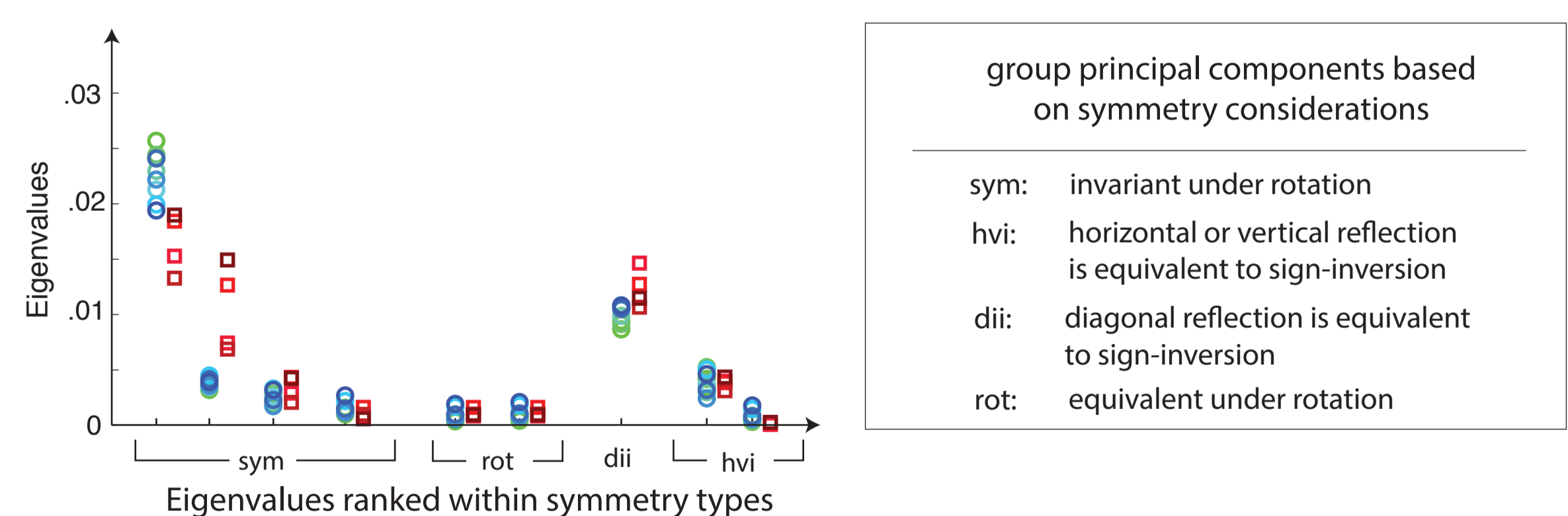
- Natural images show systematic asymmetries in β_1 versus β_- variances (upper left)
- Natural images deviate in third-order covariance plane projections (lower left)
- Natural images show asymmetries in the variances of positive versus negative image statistics, but psychophysical sensitivity does not mirror this:



Inverse Pair Covariances in Image Statistics Match Perceptual Thresholds



Principal Components of Image Statistics Match Principal Components Inferred from Psychophysical Isodiscrimination Contours



ACKNOWLEDGEMENTS

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[1] Tkačik G, Prentice JS, Victor JD and Balasubramanian, V (2010), PNAS,107(42):18149-18154. [2] Victor JD, Conte MM, Local image statistics (2012), J. Opt. Soc. Am. A, 29:1313-1345.